

Quantum Logic Programming in Prolog

Giovanni Pilato¹, Filippo Vella¹, Tommaso Brugarino², Salvatore Gaglio^{1,2}

1. Istituto di Calcolo e Reti ad Alte Prestazioni, Consiglio Nazionale delle Ricerche, via Ugo La Malfa 153, 90146 Palermo, Italy

2. Dipartimento di Ingegneria, Università di Palermo, Viale delle Scienze, ed 6,
90128 - Palermo Italy

The advantages of quantum computing can produce relevant advances in many application fields, and the development of increasingly powerful hardware platforms is enabling wider adoption of quantum solutions in real-world tasks. However, a significant limitation to applying the quantum paradigm to real problems is the difficulty in designing solutions using quantum computational blocks. We illustrate an innovative approach that allows for the description of a solution using a high-level language, which can be translated into a set of appropriate quantum gates to perform the desired computation. We present a system based on quantum computational logic proposed by Dalla Chiara et al. to represent a quantum computation within a Prolog environment. In this system, a logic formula is translated into a quantum-operable formulation, following the logic's holistic semantics. Preliminary examples illustrate the method's application.

References

- [1] Garrett Birkhoff and John Von Neumann. The logic of quantum mechanics. *Annals of Mathematics*, 37(4):823–843, 1936.
- [2] A. Chella, S. Gaglio, G. Pilato, F. Vella, and S. Zammuto. A quantum planner for robot motion. *Mathematics*, 10(14):2475, 2022.
- [3] Antonio Chella, Salvatore Gaglio, Maria Mannone, Giovanni Pilato, Valeria Seidita, Filippo Vella, and Salvatore Zammuto. Quantum planning for swarm robotics. *Robotics and Autonomous Systems*, 161, 2023.
- [4] Maria Luisa Dalla Chiara and Roberto Giuntini. Quantum logics. *Handbook of philosophical logic*, pages 129–228, 2002.
- [5] Maria Luisa Dalla Chiara, Roberto Giuntini, Roberto Leporini, and Giuseppe Sergioli. *Quantum Computation and Logic: How Quantum Computers Have Inspired Logical Investigations*. Springer International Publishing, Cham, 2018.
- [6] A. A. Markov. The theory of algorithms. *Journal of Symbolic Logic*, 18(4):340–341, 1953.
- [7] Emil L. Post. Formal reductions of the general combinatorial decision problem. *American Journal of Mathematics*, 65(2):197–215, 1943.
- [8] F. Schmalhofer and Peter Polson. A production system model for human problem solving. *Psychological Research*, 48:113–122, 01 1986.
- [9] Luis Tarrataca and Andreas Wichert. Problem-solving and quantum computation. *Cognitive computation*, 3:510–524, 2011.
- [10] A. M. Turing. On Computable Numbers, with an Application to the Entscheidungsproblem. *Proceedings of the London Mathematical Society*, s2-42(1):230–265, 01 1937.
- [11] Andreas Wichert. Quantum research with qiskit. *Mathematics*, 10(17), 2022.